

# **ShakeMovie@Home**

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# A Computational Seismology Problem

Equation of motion (2<sup>nd</sup> Newton's Law) for continuum:

$$\rho \ddot{\mathbf{u}} = \nabla \cdot \boldsymbol{\tau} + \mathbf{f}$$

density  $\rightarrow \rho$     acceleration  $\rightarrow \ddot{\mathbf{u}}$     stress  $\rightarrow \boldsymbol{\tau}$     body force (earthquake)  $\rightarrow \mathbf{f}$     elasticity tensor  $\rightarrow \mathbf{C}$

Hooke's Law:  $\boldsymbol{\tau} = \mathbf{C} : \boldsymbol{\varepsilon} = \mathbf{C} : \left\{ \frac{1}{2} [(\nabla \mathbf{u}) + (\nabla \mathbf{u})^T] \right\} = \mathbf{C} : (\nabla \mathbf{u})$

**Wave**

$$\rho \ddot{\mathbf{u}} - \nabla \cdot [\mathbf{C} : (\nabla \mathbf{u})] = \mathbf{f}$$

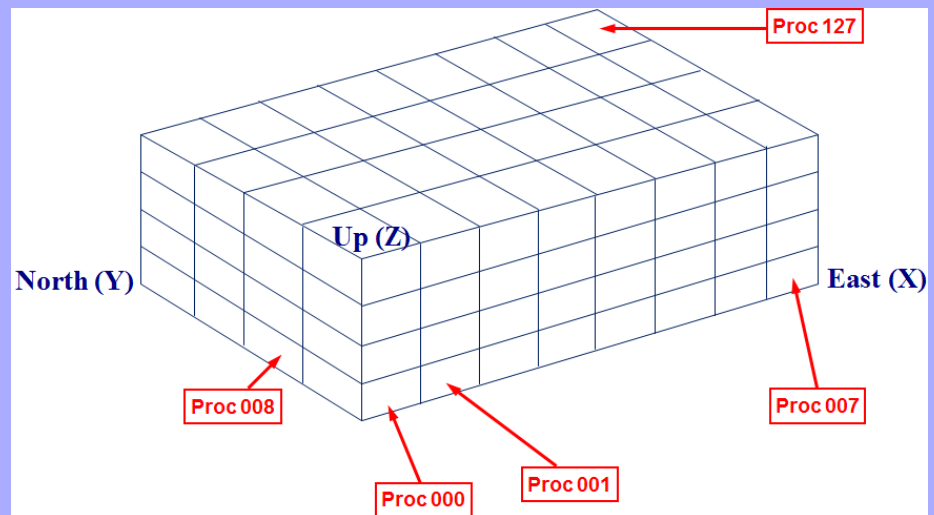
**Equation:**

**Realistic Earth model:** 3D, irregular geometry, topography

finite-difference method (FDM)

$$v_i^{n+1} = v_i^{n-1} + \frac{1}{\rho_i} \frac{\Delta t}{\Delta x} (\tau_{i+1}^n - \tau_{i-1}^n)$$

$$\tau_i^{n+1} = \tau_i^{n-1} + k_i \frac{\Delta t}{\Delta x} (v_{i+1}^n - v_{i-1}^n)$$



# Finite-Difference Simulation Parameters

(1) Spatial grid size  $h$ :  $> 5$  points per wavelength  $\lambda = v \times T$

$$\therefore h < \frac{1}{5} v_{\min} \times T_{\min}$$

speed  $\nearrow$   $\nwarrow$  period

For  $v_{\min} = 1 \text{ km/s}$ ,  $T_{\min} = 3 \text{ s}$ ,  $h = 600 \text{ m}$ . (We use  $h = 400 \text{ m}$ ).

(2) Time step  $\Delta t$ :  $\therefore \Delta t < \frac{1}{2} \frac{h}{v_{\max}}$

For  $v_{\max} = 10 \text{ km/s}$ ,  $h = 400 \text{ m}$ ,  $\Delta t < 0.02$ .

Modeling range:

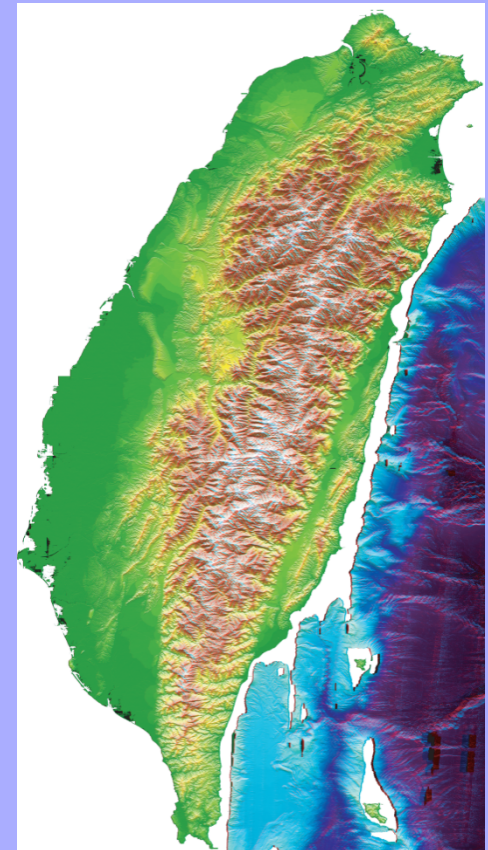
$250 \text{ km} \times 400 \text{ km} \times 80 \text{ km} \times 90 \text{ s}$

Total # of spatial-temporal grids:

$612 \times 992 \times 202 \times 4500$

CPU time and storage:

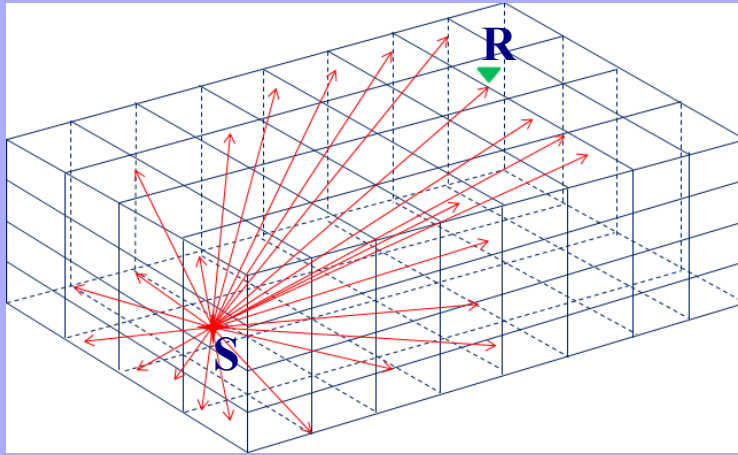
3 hours on 32 processes, 15 GB



From Y.-C. Chan

# Two Ways to Compute a Seismogram

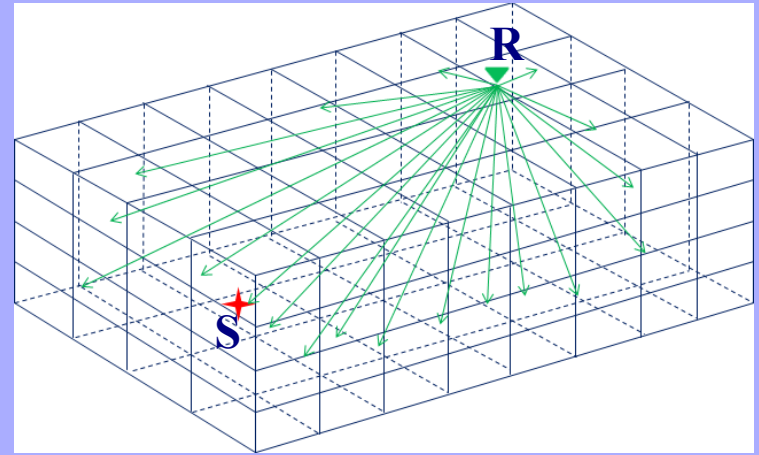
## Forward Simulation



- (1) Run simulation from earthquake  $S$ , output file includes waveforms at all grid points from the earthquake.
- (2) For a given location  $R$ , retrieve its waveform  $\mathbf{u}(S-R)$  from output file.

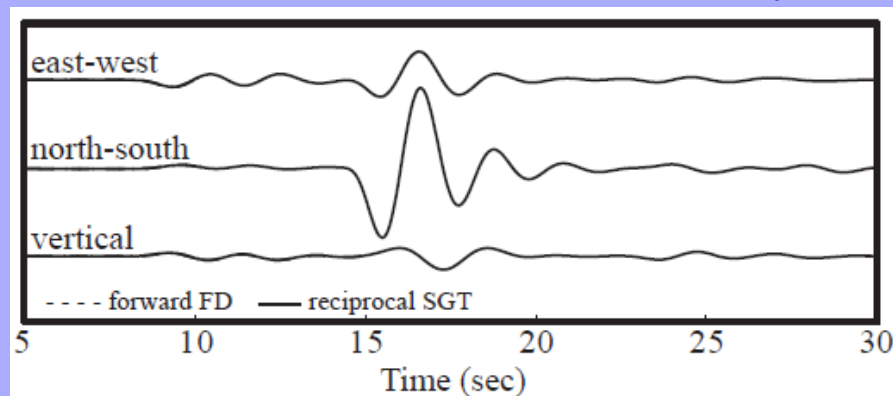
3 hrs x 32 CPUs  
15 GB

## Green's Function Reciprocity



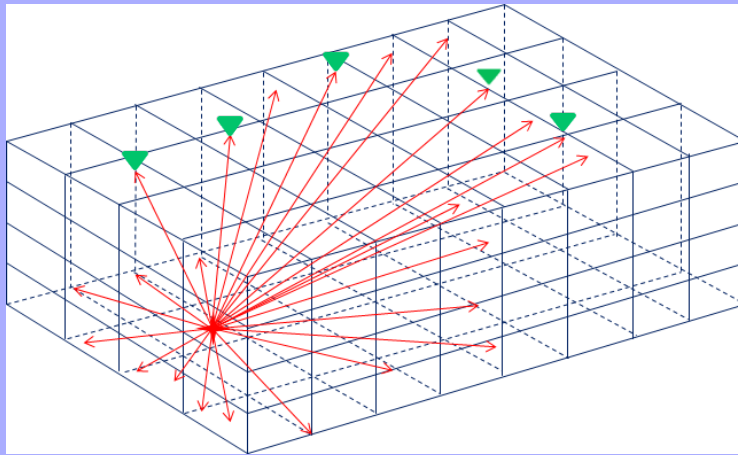
- (1) Run simulation from a location  $R$ , output file includes Green's function  $\mathbf{G}$  at all grid points from  $R$ .
- (2) For earthquake  $S$ , retrieve Green's function from  $R$  to  $S$ ,  $\mathbf{G}(R-S)$ . The waveform from  $S$  to  $R$ ,  $\mathbf{u}(S-R)$  can be easily calculated from  $\mathbf{G}(R-S)$ .

3 hrs x 32 CPUs  
15 GB



# For waveforms at 5 stations from 1 earthquake

## Forward Simulation

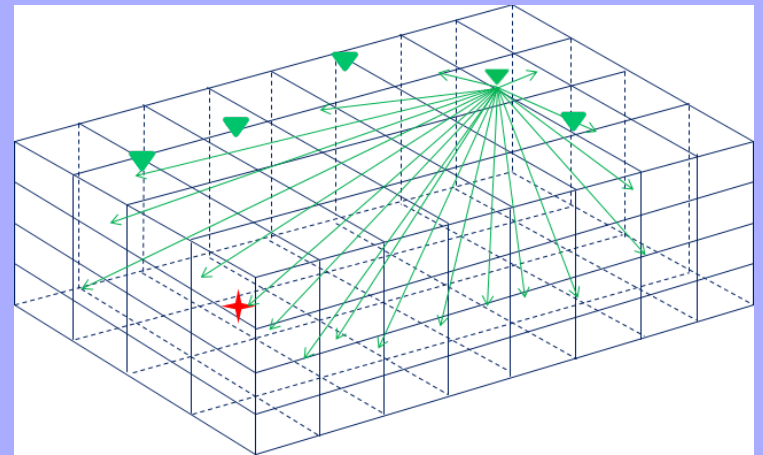


1 simulation, 5 retrievals

3 hrs x 32 CPUs

15 GB

## Green's Function Reciprocity



5 simulations, 5 retrievals

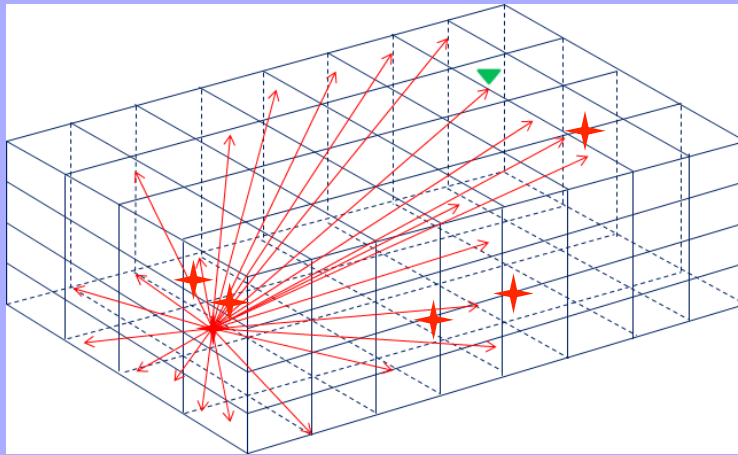
15 hrs x 32 CPUs

75 GB

**Decision: Forward simulation!**

# For waveforms at 1 station from 5 earthquakes

## Forward Simulation

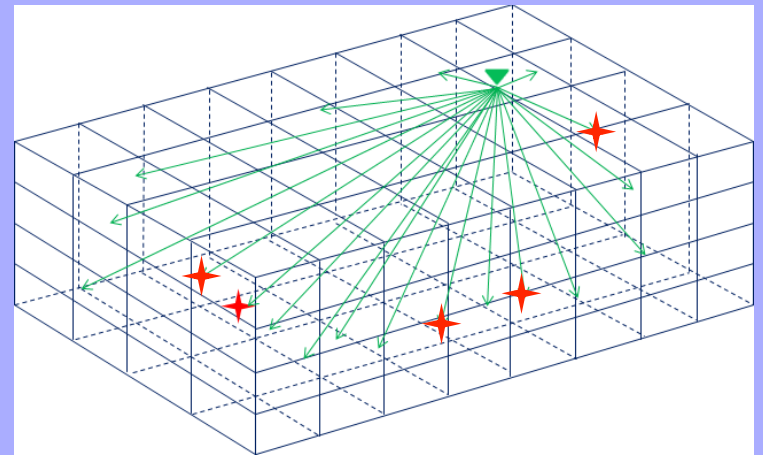


5 simulations, 5 retrievals

15 hrs x 32 CPUs

75 GB

## Green's Function Reciprocity



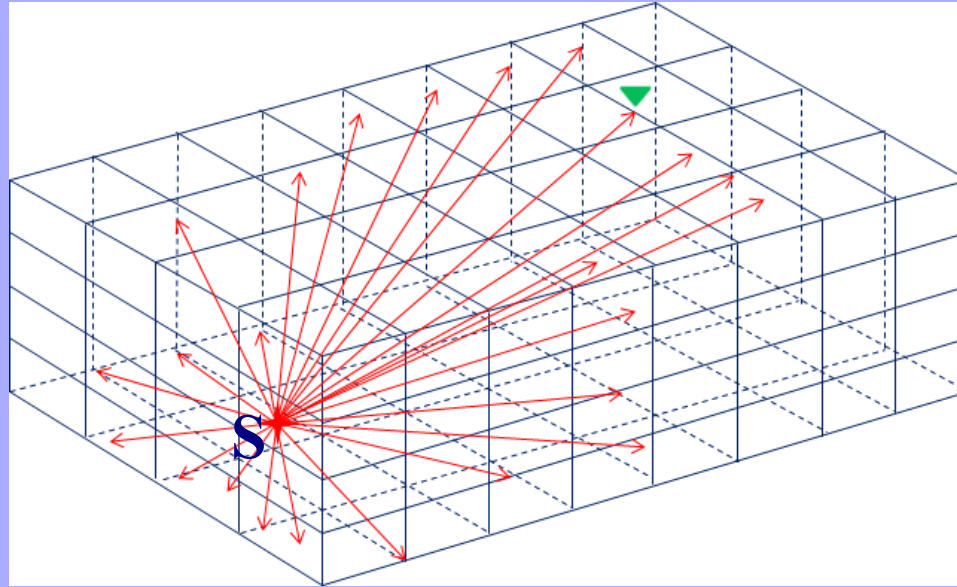
1 simulation, 5 retrievals

3 hrs x 32 CPUs

15 GB

**Decision: Green's function!**

# Shake Movie Production



Given earthquake S, we need waveforms at a large number of points on the surface (7168 for Taiwan).

Forward simulation: 1 simulation (3hrs.) and 7168 retrievals.



# Caltech's So. Cal. ShakeMovie

From: Notification of movies of recent seismic events. <shakemovie-notify@caltech.edu>  
To: shakemovie-notify@caltech.edu  
Subject: [ShakeMovie] Magnitude 4.1 :: 9 miles N of Ocotillo, CA :: Thu Nov 4 19:39:59 2010 UTC [Add Tag]  
Date: Thu, 04 Nov 2010 14:32:00 -0700 (PDT)

EMAIL NOTIFICATION  
shakemovie.caltech.edu  
Event Id:10832573

There is new media now available for download on the recent seismic event:

Magnitude: 4.1  
9 miles N of Ocotillo, CA  
UTC: Thu Nov 4 19:39:59 2010  
Latitude: 32.87  
Longitude: -116.02

All movies for this event are available from:

<http://shakemovie.caltech.edu/event?evid=10832573>

The movies available include:

## SOUTHERN CALIFORNIA

<http://shakemovie.caltech.edu/dl?evid=10832573&product=socal&style=orange&size=small>

## LOS ANGELES BASIN

<http://shakemovie.caltech.edu/dl?evid=10832573&product=la&style=orange&size=small>

To unsubscribe, visit <http://shakemovie.caltech.edu/signup>.

You will see an Email Password and Unsubscribe buttons at the bottom left.

This email was automatically generated by Caltech's Southern California  
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(( ( shakemovie.caltech.edu ) ))

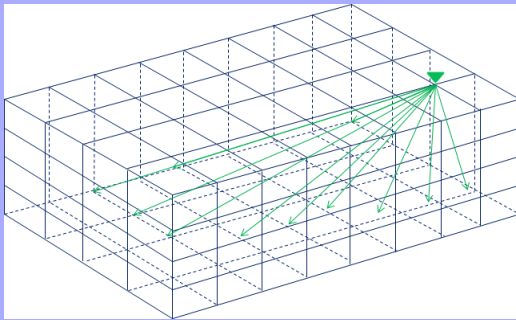
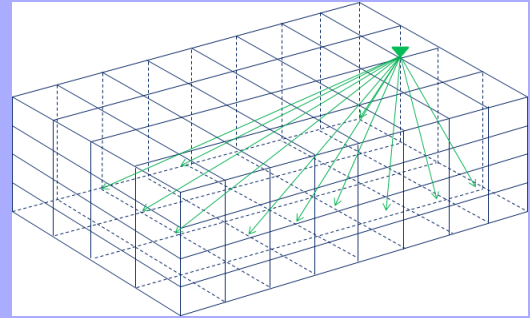
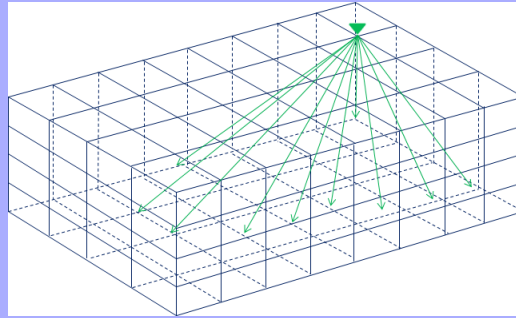
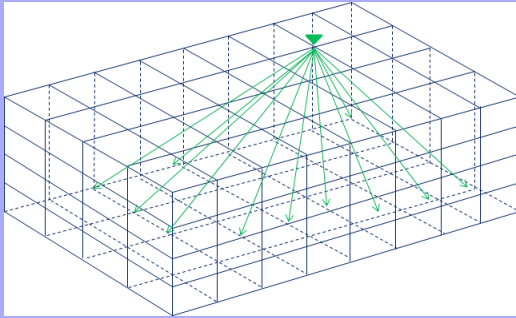




# **Near Real-Time Waveforms and ShakeMovie**

Can we have shake movies faster?

# Green's Function Database



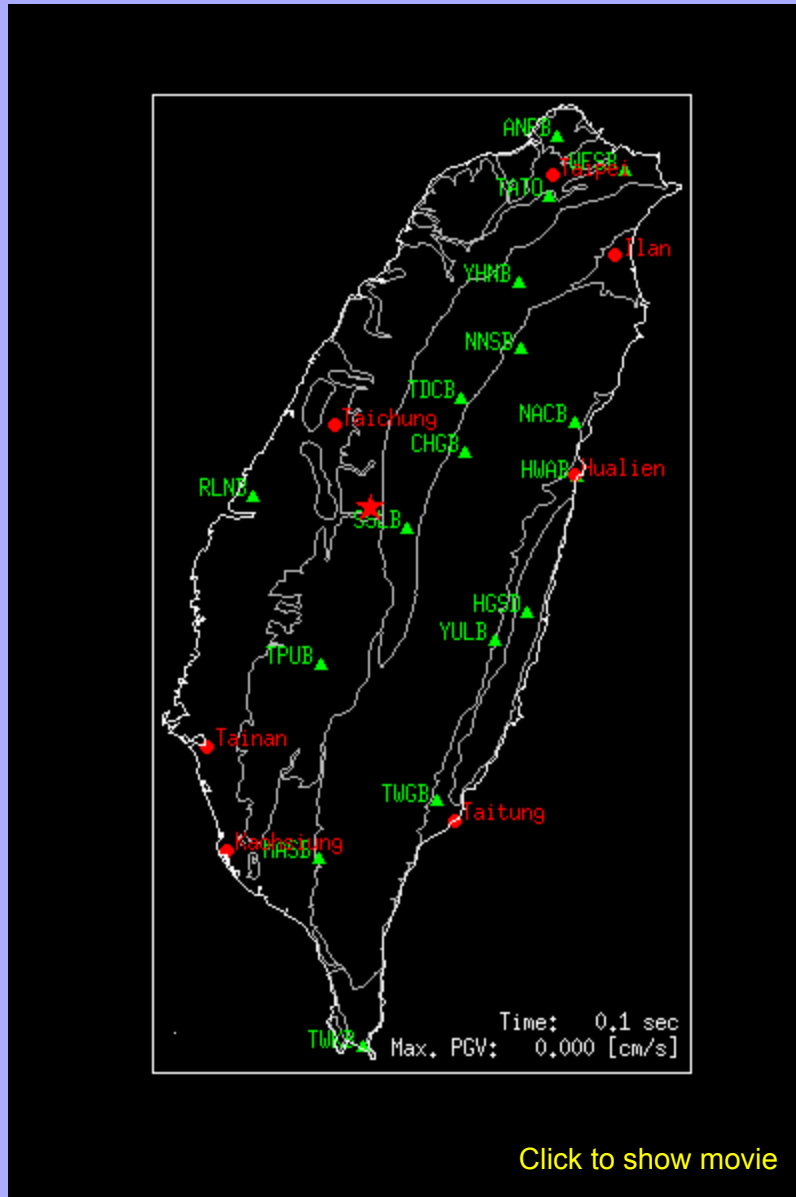
Run 7168 simulations to obtain Green's functions for all surface grid points. Establish Green's function database.

**CPU:** 7168 x 3 hrs. on 4 nodes (32 cores) or 45 days on 80 nodes.

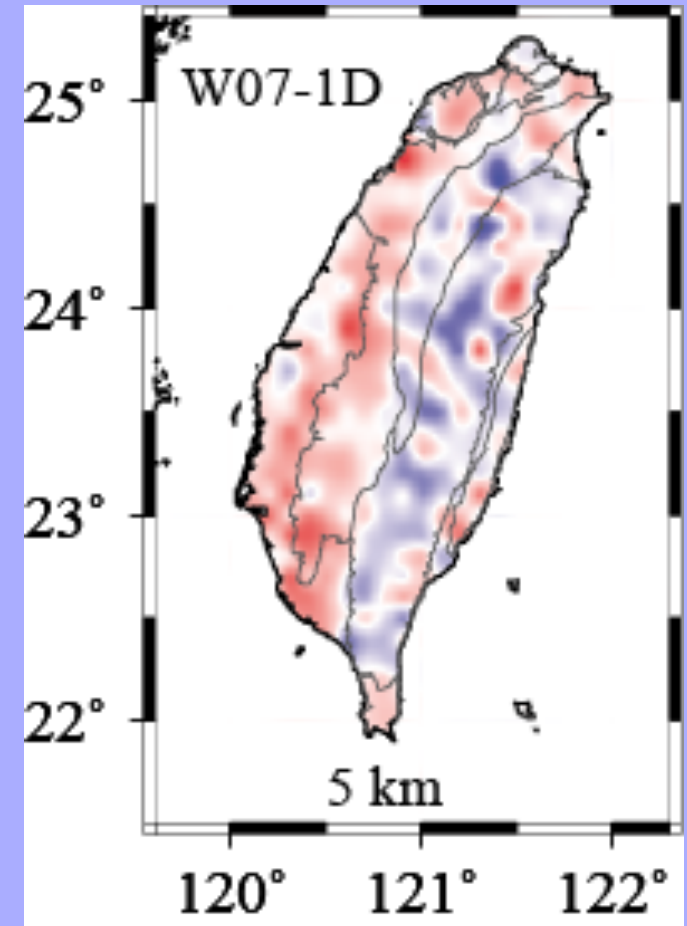
**Storage:** 7165 x 15 GB or ~100 TB.

No simulation is required for waveform and shakemovie calculations for future earthquakes! Only retrievals are needed

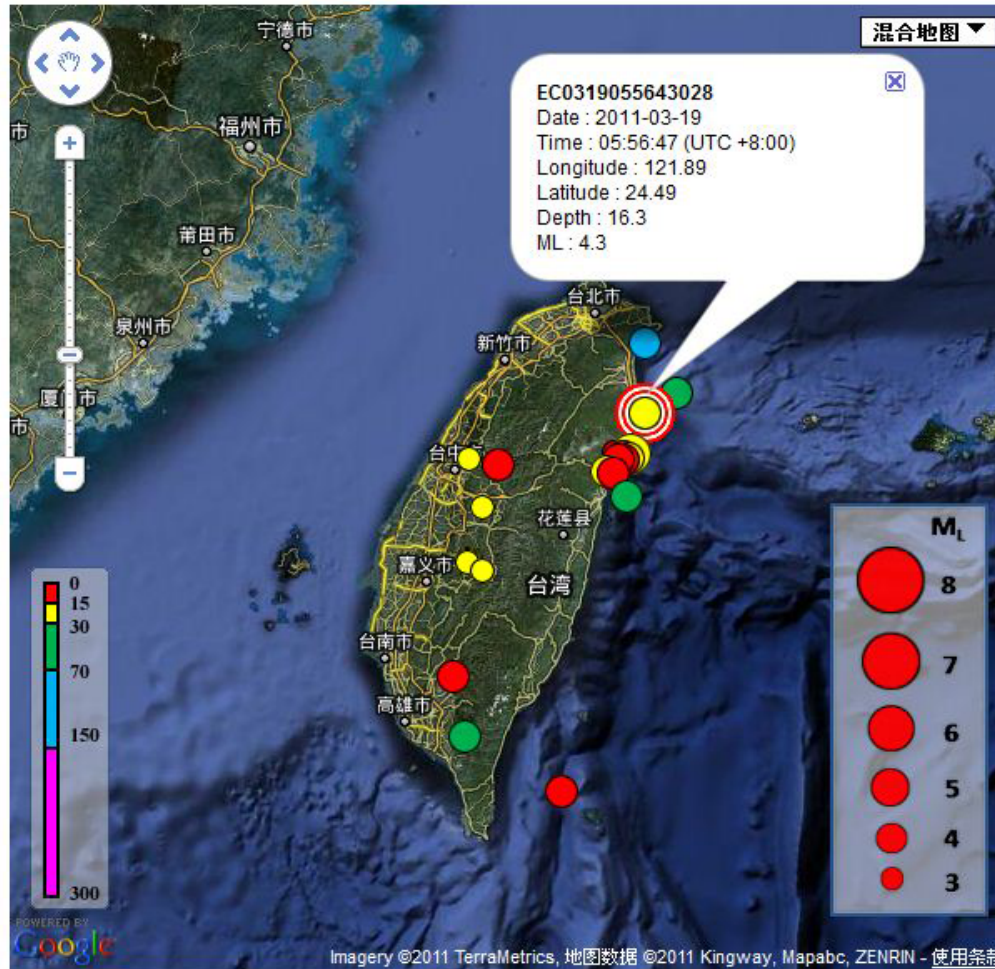
# Shake Movie: Chi-Chi (Taiwan) Earthquake



Near-surface velocity



# CMT Solutions at Taiwan Earthquake Center

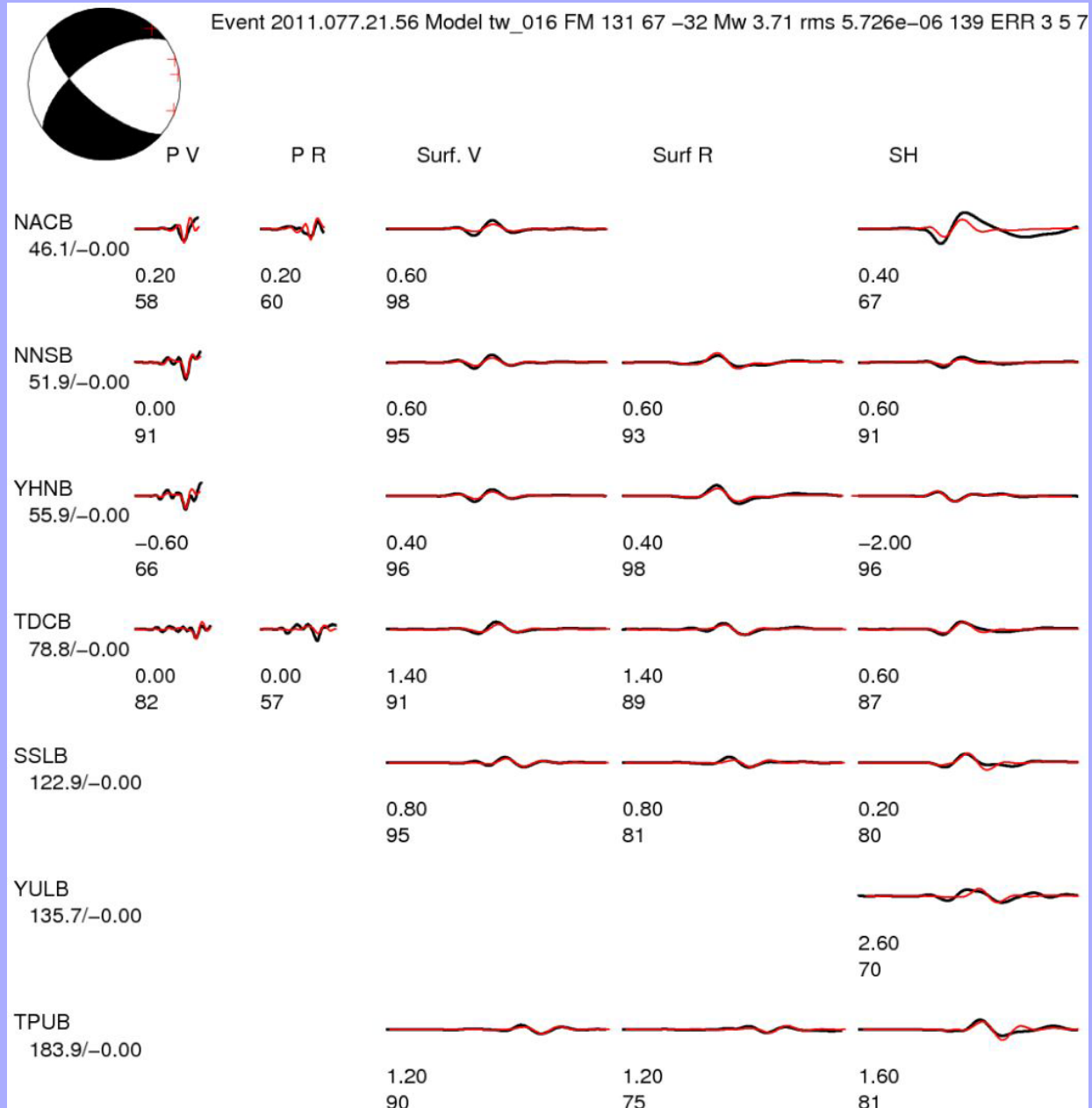


2011.077.21.56



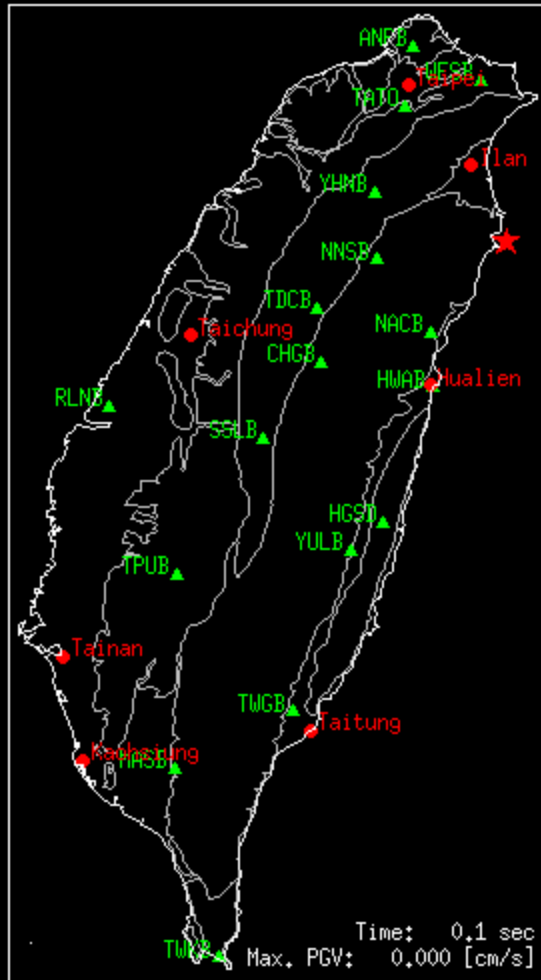
Automatic, available  
~2 min. after alert

# Observed (black) and Predicted (red) Waveforms



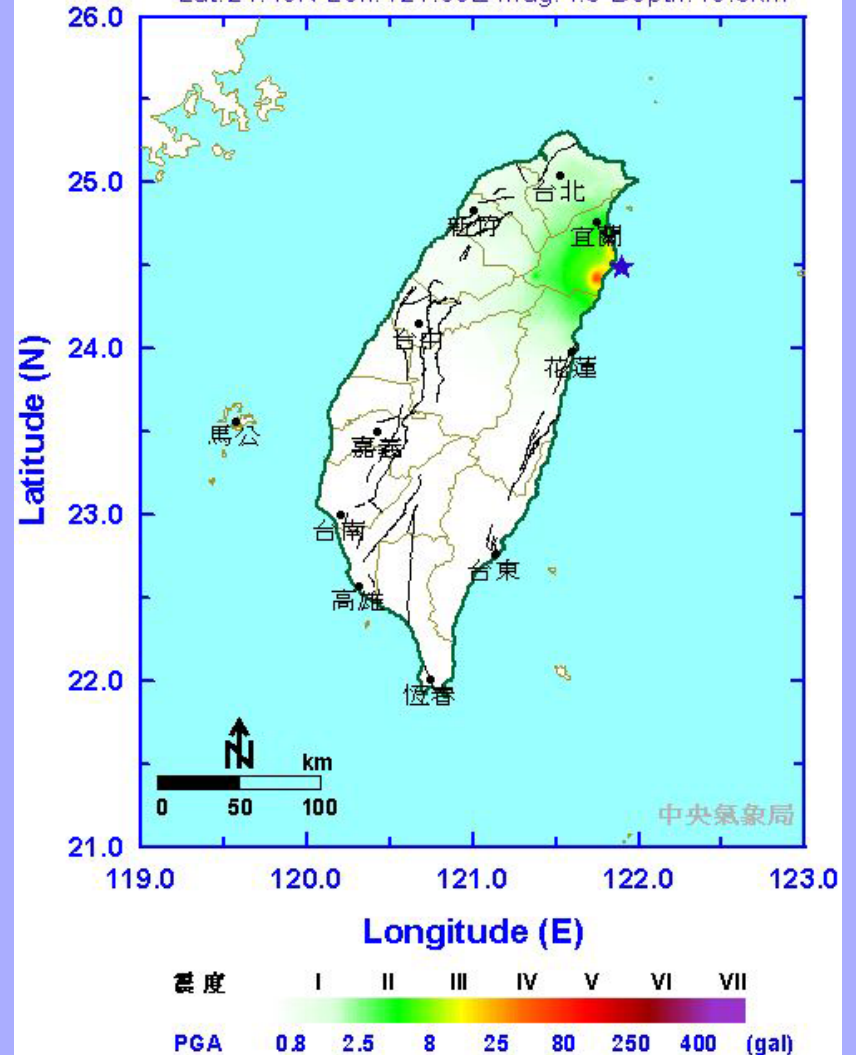
# Shake Movie

## CWB Strong Motion Observation



[Click to show movie](#)

Origin Time: 2011/03/19 05:56:46 (GMT+08:00)  
Lat: 24.49N Lon: 121.89E Mag: 4.3 Depth: 16.3km





# ShakeMovie@Home

- Distribute the 7168 Green's functions (15GB each): up to 7168 sites.
- Distribute Green's function retrieval (21KB each): up to 7168 volunteers' desktops/laptops.
- Greater distribution enables consideration of more detailed features (higher frequency/resolution).
- All waveforms and shake movies can be available within minutes after earthquake alert.

# Further Improvements

- Improve I/O performance.
- Higher frequency and resolution: smaller grid size.
- Accuracy: near-surface site condition, topography.

**Thank you!**